

## Accelerated Multidimensional NMR Data Acquisition by Varying the Pulse Sequence Repetition Time

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Received February 12, 2009; E-mail: macura@mayo.edu

It has been recognized that the versatility of multidimensional (mD) Fourier transform (FT) NMR experiments<sup>1</sup> is enhanced when the data accumulation time is reduced. To date, such reduction has been achieved by numerous techniques, from evolution period shortening<sup>2–4</sup> and/or evolution parallelization<sup>5,6</sup> to the complete elimination of repetition time ( $T_R$ ).<sup>7</sup>

To reduce the duration of mD experiments, I propose variation of the pulse sequence repetition time (VRT) in concert with sampling of evolution domain(s). In this approach, an experiment starts with the usual repetition time ( $T_{R0} \approx 1 - 5T_1$ ) and ends with  $T_R \ll T_1$ , resulting in a considerable reduction of the length of data acquisition. If  $T_{R0} \geq 5T_1$ , equilibrium peak volumes are also preserved.

The total repetition time is the sum of the individual periods  $T_{Ri}$ , i.e.,  $N_S \sum_{i=1}^{N_I} T_{Ri}$ , where  $N_S$  is the number of scans and  $N_I$  the number of increments. With constant  $T_R$ , the total repetition time is  $N_I N_S T_R$ . In the VRT experiment,  $T_R$  becomes a function of evolution time  $t_1$ , i.e.,  $T_{Ri} = f(t_{1i})$ . If  $f(t_{1i})$  is chosen such that its time average  $\bar{f}(t_1)$  is smaller than  $T_{R0}$ , the duration of the experiment is reduced by  $T_{R0}/\bar{f}(t_1)$ . Other delays unaffected by VRT, denoted by  $\sum d$ , render the total effect somewhat smaller, with a time reduction of  $(T_{R0} + \sum d)/[\bar{f}(t_1) + \sum d]$ .

The magnitude of the steady-state longitudinal magnetization depends on the repetition time  $T_R$  as  $1 - \exp(-T_R/T_1)$ . In the evolution domain, the magnetization decays exponentially as  $\exp(-t_1/T_2)$  with relaxation time  $T_2$ . If  $T_R$  is modulated by an arbitrary function  $f(t_1)$  in parallel with the evolution time, the normalized magnetization  $M_r = M/M_0$  is given by

$$M_r(t_1) = \{1 - \exp[-f(t_1)/T_1]\} \exp(-t_1/T_2) \quad (1)$$

The VRT term multiplies the  $t_1$  free induction decay (FID) in analogy to the filtering function in data processing. Thus, eq 1 can be viewed as filtering along the evolution domain during data acquisition. In addition to the time savings, which depends on the time average  $\bar{f}(t_1)$ , one can select the VRT function to enhance resolution or achieve any other effect related to the line shape in the evolution domain. In 3D or higher-dimension experiments, line widths in the evolution domain are most often determined by the domain length rather than the natural line width, i.e.,  $t_1^{\max}/T_2 \ll 1$ . In this case, the line broadening caused by VRT is minimal (or negligible) compared with the broadening by subsequent filtering in the course of processing. In addition, the repetition time is often shorter than the relaxation time ( $T_R < T_1$ ). When this is true, the  $T_2$  term can be omitted, so to a first approximation, eq 1 can be simplified to

$$M_r(t_1) \approx 1 - \exp[-f(t_1)/T_1] \approx f(t_1)/T_1 \quad (2)$$

Equation 2 shows that (with rapid pulsing) the magnetization amplitude during the evolution time follows the actual VRT

function. This simplifies the selection of  $f(t_1)$  to functions that would be used anyway to apodize the  $t_1$  FID in the standard experiment. When  $f(t_1)/T_1 > 1$ , the full exponential form must be used in eq 2; eventually, with the VRT function decay, the linear approximation becomes valid again. Thus, when  $f(t_1)/T_1 \geq 5$ , the initial magnetization is constant [i.e., equal to the equilibrium magnetization ( $M_r = 1$ )], so it enters the linear approximation regime when  $f(t_1) \ll T_1$ .

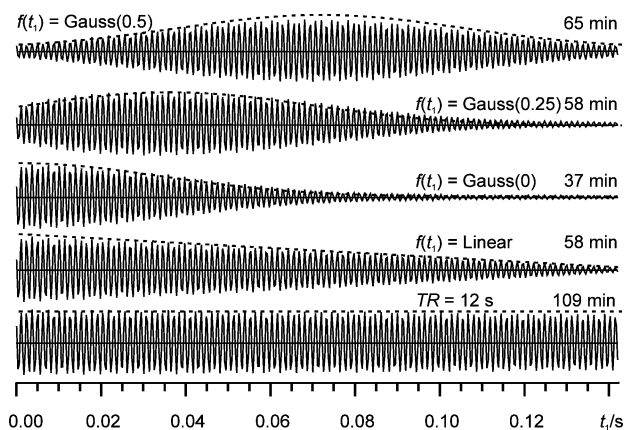
I used a 10 mM sucrose solution in  $D_2O$  (prepared by two cycles of freeze-drying and dissolving in “100 percent”  $D_2O$ ) to demonstrate the basic properties of the VRT method. At 600 MHz and 25 °C (using a Bruker Avance spectrometer equipped with a cryoprobe), the residual HOD protons were characterized by  $T_1 = 20.4$  s and  $T_2 = 0.50$  s; with repetition time of 12 s and an evolution time of 0.13 s, these relaxation times satisfy the conditions under which eq 2 was derived [ $f^{\max}(t_1)/T_1 \leq 0.6$ ,  $t_1^{\max}/T_2 \leq 0.26$ ]. I implemented the VRT method by substituting variable-delay lists for the fixed delays ( $T_R$  and  $t_m$ ) in the pulse sequences. When both  $T_R$  and  $t_m$  were varied, I used the variable counter list as well. To eliminate interferences of residual transverse magnetization from previous scans, a small gradient pulse at the beginning of the relaxation delay (or the end of acquisition) was inserted.

Figure 1 shows the results of an experimental test of eq 2 in which traces of  $t_1$  FIDs (solid lines) of the residual HOD signal are compared with the respective  $f(t_1)$  values (dashed lines) obtained from a series of VRT–TOCSY experiments on the sucrose sample. As expected, the FIDs of the residual solvent signal followed the respective VRT functions rather closely.

To test the VRT method further, I implemented it in a NOESY–HSQC 3D experiment in which I modulated  $T_R$  and  $t_m$ . Again I used 10 mM sucrose, where the natural abundance makes the solution 0.1 mM in  $^{13}C$ . In addition to the low  $^{13}C$  concentration, the nuclear Overhauser effects (NOEs) in sucrose are comparatively weak (and positive), rendering detection of cross-peaks somewhat challenging. Figure 2 shows the Glc–H<sub>1</sub>  $^1H$  vector from a series of VRT–NOESY–HSQC 3D spectra recorded with different VRT functions. The VRT modulation was applied in both the  $t_1$  and  $t_2$  domains, implying that both  $T_R$  and  $t_m$  were continuously shortened by departure of either  $t_1$  or  $t_2$  from zero ( $t_3$  is the detection time). Noticeable in Figure 2 is the line narrowing and improved signal-to-noise ratio (SNR) of the diagonal (Glc–H<sub>1</sub> → Glc–C<sub>1</sub>) in the VRT experiments relative to an otherwise identical experiment recorded with constant  $T_R$ . The SNR for the cross-peak (Glc–H<sub>2,4</sub> → Glc–H<sub>1</sub> → Glc–C<sub>1</sub>) remained almost constant, even though the experiments took half the time. Here the narrowing of the diagonal line was caused by shortening of the mixing time rather than by  $T_R$  modulation, in complete analogy to the ACCORDION experiment.<sup>8</sup> The cross-peak was affected only minimally because its buildup curve is rather flat around 1 s.

In theory, the VRT method accelerates data acquisition at the expense of SNR: a shorter  $T_R$  at the outskirts of the indirect domain weakens the observable signal with no effect on the noise. However,

because of the finite length of delays unaffected by VRT (acquisition, mixing, dephasing/rephasing, etc.), the signal is appreciable even with  $f(t_1) = 0$ . This means that data apodization must be applied in any case, thus attenuating any unfavorable VRT effects.

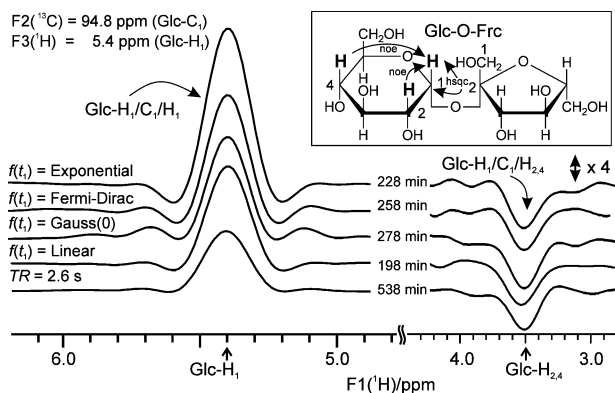


**Figure 1.** Free induction decay of the residual HOD signal (10 mM sucrose in  $D_2O$ ) in a series of VRT-TOCSY experiments with the indicated VRT functions. Numbers of minutes indicate total durations of the experiments. The number in the Gaussian VRT function indicates the fractional position of the maximum within the time domain. In each case,  $f^{\max} = 12$  s.

In the VRT experiment, the spin system never reaches the steady state because a distinct  $T_R$  characterizes each evolution increment. Thus, acquisition of more scans at any given increment would require cycling through  $T_R$  values rather than through the pulse phase and/or receiver phase. However, most often this is unnecessary because the  $T_R$  changes between successive evolution increments are rather small. For example, with linear increments in VRT and  $N_1$ , the  $T_R$  change  $[f(0)/N_1]$  is usually less than the SNR in a given FID. Consequently, in most experiments, implementation of VRT requires only replacing the fixed  $T_R$  by a variable delay. If the acquisition domain is short, then the residual transverse magnetization should be removed by a small gradient after the acquisition. If a gradient is not available, then random modulation of the whole set of phases between successive scans (keeping the relative phases constant within the scan or as required by phase rotation) will send potential artifacts into the background noise. The only apparent limitation of the VRT method is that it cannot be implemented in experiments that require a long  $T_R$  (e.g., for preirradiation).

The VRT method works well for molecules of all sizes (small molecules to macromolecules), often cutting the total experiment time in half without any artifacts. In fact, in small- and medium-sized molecules where there is no spin diffusion, the VRT method can shorten the mD acquisition time without affecting the spectrum at all. In such cases,  $^{13}C$ -bound protons can be characterized by shorter  $T_1$ 's than  $^{12}C$ -bound protons (used for  $T_R$  estimate), so the  $T_R$ 's tend to be overestimated.

The VRT method can be applied in numerous forms. For example, by a suitable choice of the VRT function, one could either sculpt the evolution line shapes or use the function as a  $T_1$  filter to selectively broaden the lines with long  $T_1$ 's or transmit  $T_1$  information into evolution line widths. VRT could be applied in concert with sampling of one or all of the evolution domains, with the mixing period, or with any of their combinations. The ability of the VRT method to preserve the equilibrium magnetization by



**Figure 2.** Proton vector from VRT-NOESY-HSQC 3D spectra of 10 mM sucrose in  $D_2O$  taken at the  $F_2(^{13}C)$  frequency of Glc- $C_1$  and  $F_3(^1H)$  of Glc- $H_1$ . Because of the low digital resolution in the 3D spectra of Glc- $H_{2,3}$ , the resonances are not resolved. Magnetization flows from  $H_{2,3}$  to  $H_1$  via an NOE (in sucrose, the NOE is positive, thus giving a negative cross-peak) and then, for frequency labeling, via single-quantum coherence between  $H_1$  and  $C_1$ , as indicated by the arrows in the structure. The total experiment time is expressed in minutes. Experiments were performed with the VRT functions indicated at the left and used to vary both  $T_R$  and  $t_m$  simultaneously. In each case,  $f^{\max} = 2.6$  s.

starting the experiment with  $f(0) \geq 5T_1$  is particularly useful in quantitative mD spectroscopy (e.g., EXSY, NOESY), as will be shown elsewhere.

Because of its close analogy to filtering, the VRT method should be used with caution, as with all filtering functions. In addition, an extremely fast repetition rate can introduce spectral distortions specific to the spectrometer (the VRT function should acknowledge a duty cycle limitation for a given system) and the sample (sample overheating due to duty-cycle shortening). However, the principal advantage of the VRT is in reduced data acquisition time in mD experiments with minimal alteration of existing pulse sequences.

It is noteworthy that VRT can be combined with other acceleration methods for even better results. For example, one could easily create the VRT-SOFAST hybrid, in which the excitation pulse width is modified in concert with the changing repetition time. This combination of methods will enable a smooth transition from the normal 2D regime (low speed, no distortion) through the VRT-SOFAST regime to the SOFAST regime.

**Acknowledgment.** I thank Dr. Stanimir Vuk-Pavlović for useful suggestions and critical reading of the manuscript.

**Supporting Information Available:** Acquisition and processing details for Figures 1 and 2, plots of the VRT functions used, and  $^1H$ - $^{15}N$  VRT-HMQC spectra of ubiquitin. This material is available free of charge via the Internet at <http://pubs.acs.org>.

## References

- Ernst, R. R.; Bodenhausen, G.; Wokaun, A. *Principles of Nuclear Magnetic Resonance in One and Two Dimensions*; Oxford University Press: New York, 1990.
- Zhu, G.; Bax, A. *J. Magn. Reson.* **1992**, *98*, 192–199.
- Hu, H. T.; De Angelis, A. A.; Mandelshtam, V. A.; Shaka, A. J. *J. Magn. Reson.* **2000**, *144*, 357–366.
- Rovnyak, D.; Frueh, D. P.; Sastry, M.; Sun, Z. Y. J.; Stern, A. S.; Hoch, J. C.; Wagner, G. *J. Magn. Reson.* **2004**, *170*, 15–21.
- Atreya, H. S.; Szyperski, T. *Proc. Natl. Acad. Sci. U.S.A.* **2004**, *101*, 9642–9647.
- Kupce, E.; Freeman, R. *J. Am. Chem. Soc.* **2004**, *126*, 6429–6440.
- Schanda, P.; Brutscher, B. *J. Am. Chem. Soc.* **2005**, *127*, 8014–8015.
- Bodenhausen, G.; Ernst, R. R. *J. Am. Chem. Soc.* **1982**, *104*, 1304–1309.

JA9011063